

Since $\hat{\mathbf{n}} = -\hat{\mathbf{i}}$ at the face at $x = 0$, the surface charge density at $x = 0$ is given by

$$\sigma_b|_{x=0} = \bar{\mathbf{P}} \cdot \hat{\mathbf{n}}|_{x=0} = -\bar{\mathbf{P}} \cdot \hat{\mathbf{i}} = -(ax^2 + b)|_{x=0} = -b \quad (\text{ii})$$

Since $\hat{\mathbf{n}} = \hat{\mathbf{i}}$ at the face $x = L$, the surface charge density at $x = L$ is

$$\sigma_b|_{x=L} = \bar{\mathbf{P}} \cdot \hat{\mathbf{n}}|_{x=L} = \bar{\mathbf{P}} \cdot \hat{\mathbf{i}} = (ax^2 + b)|_{x=L} = (aL^2 + b) \quad (\text{iii})$$

Since $dV = A dx$, using Eq. (i), we get the total bound volume charge as

$$Q_b^V = \int_V \rho_b dV = \int_0^L (-2ax) A dx = -aAL^2$$

Using Eq. (ii), we get the bound surface charge on the surface S_1 at $x = 0$ as



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